



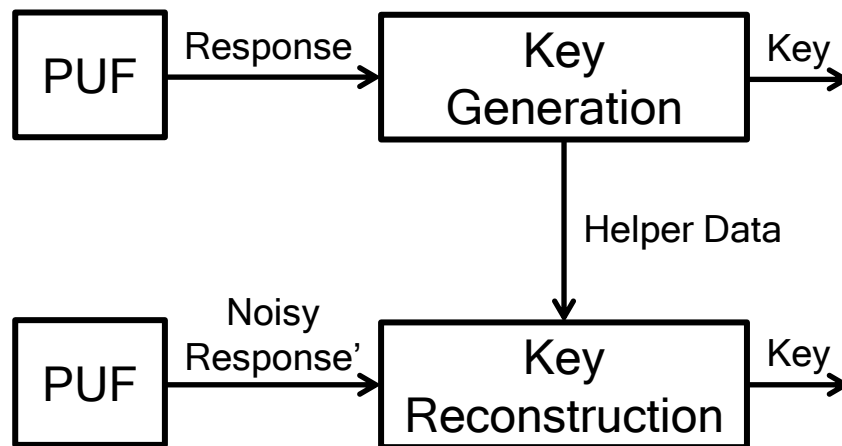
Secure Key Generation from Biased PUFs

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Introduction

- PUF-based key generation



- Reliability:

If Response \approx Noisy Response **then** Key = Key'

- Security:

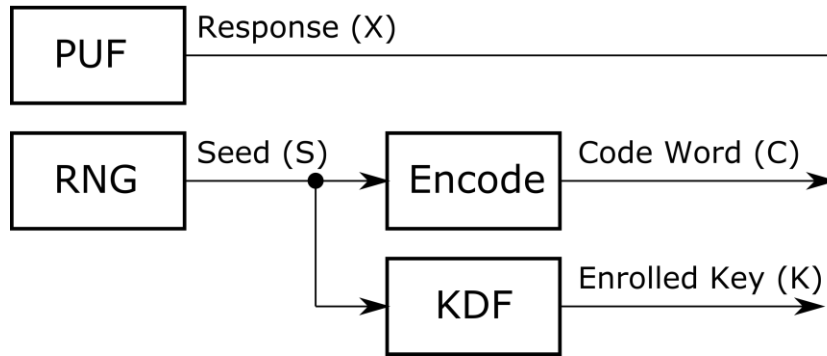
If Response is sufficiently unpredictable (w.r.t. its length) **then** Key is fully unpredictable, **even though** Helper Data is known

- What if PUF response is not full-entropy?

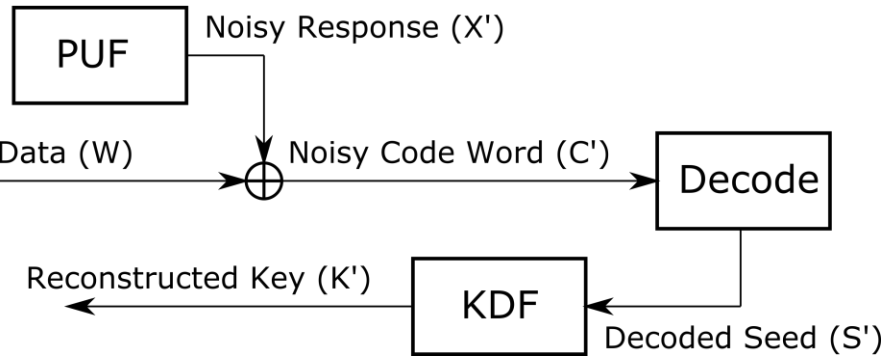


Setting: PUF-based Key Generation

Enrollment:



Reconstruction:



- Code-offset construction

- Helper data = offset between PUF response and random code word
- Key = derived from random seed which determines code word

- Security?

- $KDF(.)$ = cryptographically secure key derivation function
- S = input with sufficient entropy to derive a key from

- $H(S | W) = ?$

- $H(S | W) = H(S) - I(S ; W) = |S| - I(S ; W) = |S| - I(S ; X + Encode(S)) = ?$



Leakage Problem: General

- $H(S | W) = \underbrace{|S|}_{\text{Initial Seed Entropy}} - \underbrace{I(S ; W)}_{\text{Entropy Leakage}} = \text{Entropy left for key derivation}$

Initial Seed Entropy

Entropy Leakage

- **Entropy leakage?**

- $I(S ; W) = I(S ; X + S^*G)$ (G = generator matrix of block code)
- $= |S| - [H(X) - H(X^*H^T)]$ (H = parity-check matrix)

- If X fully random ($H(X) = |X|$), then $I(S ; W) = 0$
→ no entropy leakage! and $H(S | W) = |S|$

- **If X not fully random, then $I(S ; W) \geq 0$**
→ possible entropy leakage and $H(S | W) = H(X) - H(X^*H^T)$

- $H(X^*H^T) = ?$

- Depends on distribution of X and on code structure H^T

- Difficult to compute exactly for the general case

- Upper bound: $H(X^*H^T) \leq |X^*H^T| = (n - k)$ (for an (n, k) block code)

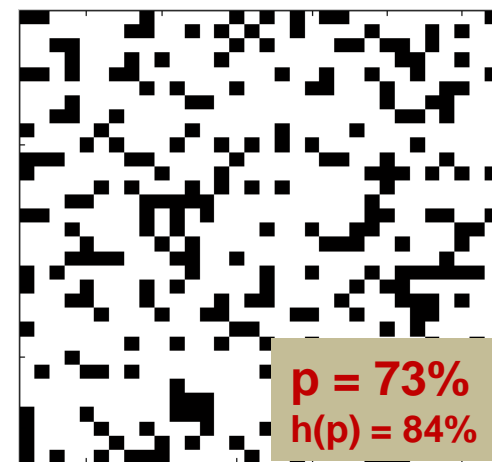
- → results in upper bound on leakage, or lower bound on remaining entropy



Leakage Problem: Bias Only

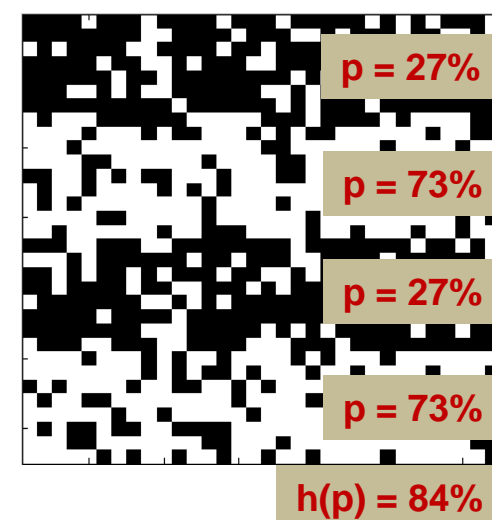
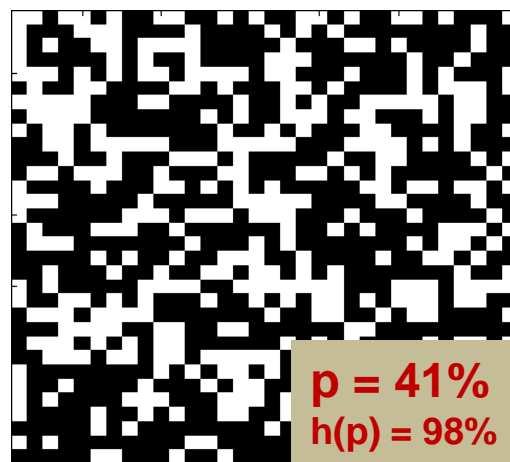
- X in $\{0,1\}^n$ not fully random because of bias only

- Most common and obvious cause of PUF non-randomness
- p -biased PUF \rightarrow for an unseen response bit $Pr(X_i = 1) = p$
- $H(X) = n \cdot h(p)$
($h(\cdot)$ = binary entropy function)



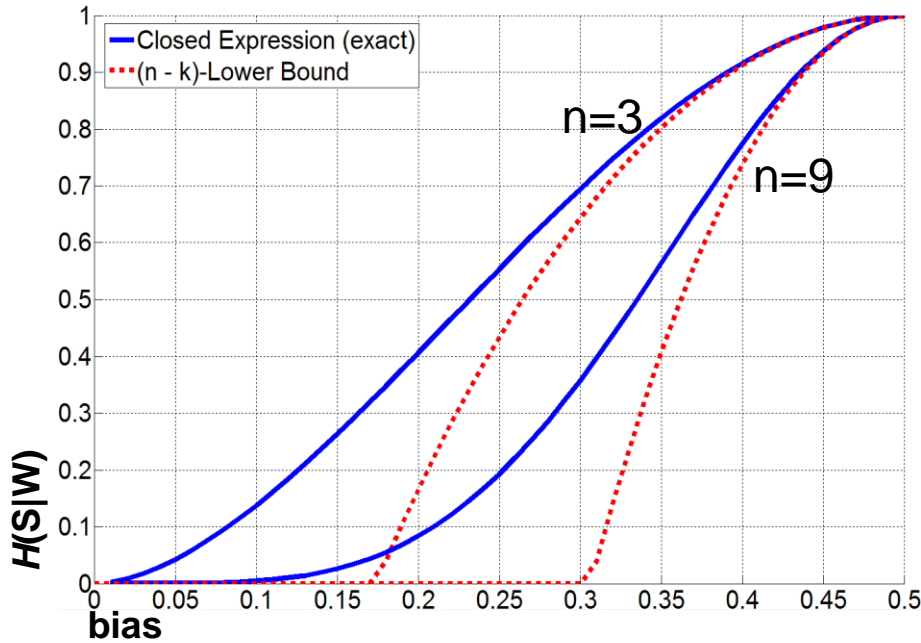
- $H(X^*H^T) = ?$

1. For simple codes (e.g. repetition) \rightarrow closed expression
2. For short codes (e.g. $n < 32$) \rightarrow exhaustively determine distribution of X^*H^T
3. Otherwise \rightarrow use upper bound ($n - k$)



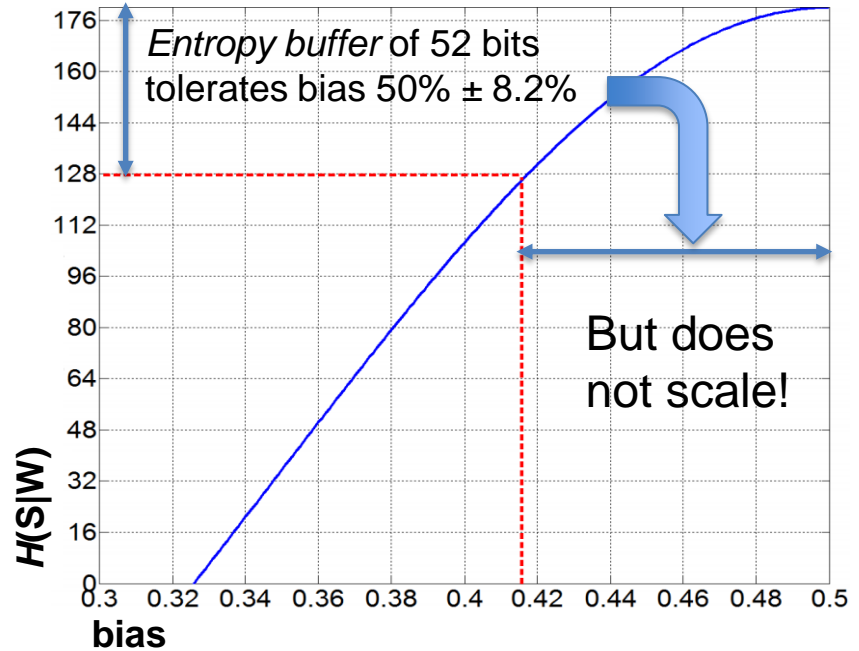
Leakage Problem: Effect of Bias

- For repetition codes:



- Lower bound very pessimistic for bias not close to 50% (cf. "repetition code pitfall", Koeberl et al., HOST-2014)
- But still significant entropy loss due to bias

- For full key generator (ex.):

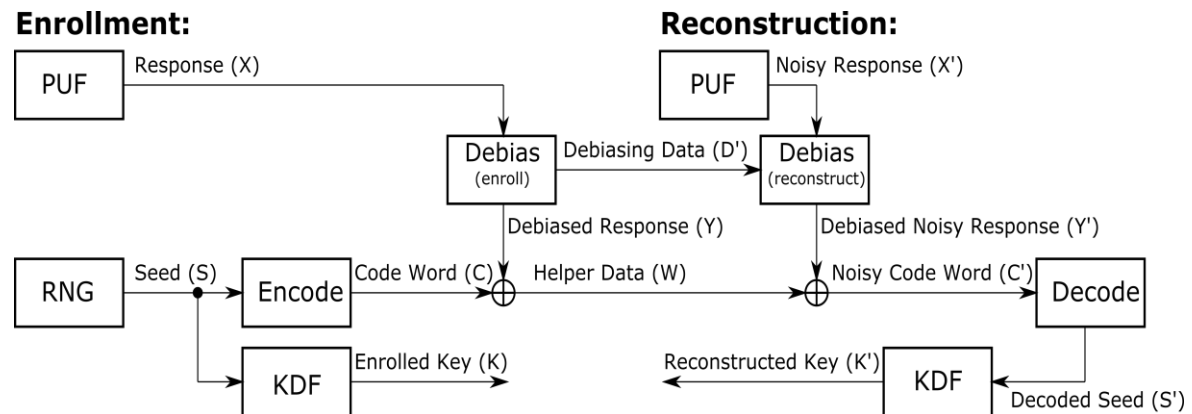
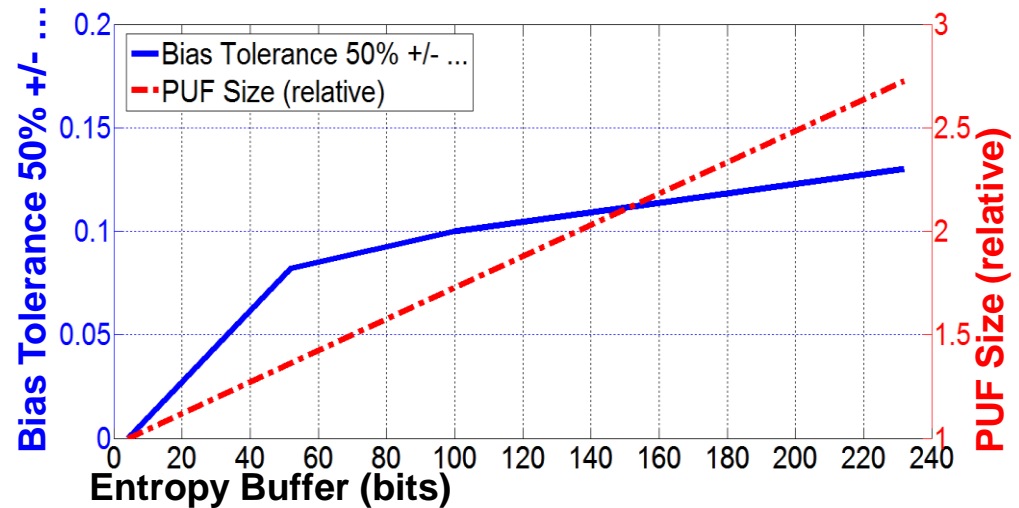


- Based on concatenated Repetition(8,1) o Golay(24,12) code (van der Leest et al., CHES-2012)
- Generates 128-bit key with $>1 \cdot 10^{-6}$ reliability in presence of $<15\%$ noise
- **Secure for 41.8% < bias < 58.2%**

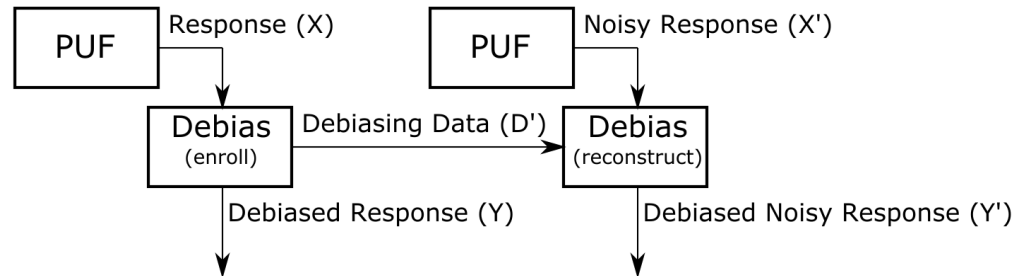


Solution: Debiasing

- Bias tolerance does not scale with entropy buffer
 - PUF size does scale with entropy buffer!
 - Bias tolerance limited even when buffer $\rightarrow \infty$
- Other solution needed
 - For bias levels above limit
 - For PUF size efficiency
- **Debiasing** prior to code-offset
 - Debiasing (helper) data



Solution: Criteria



1. Reliability

Debiasing cannot compromise reliability of key generation
(e.g. $\text{hash}(X)$ removes bias but blows up bit error rate of PUF response)

2. Efficiency

If $|Y| < |X|$ then debiasing induces overhead
→ debiasing overhead should be limited and as small as possible

3. Leakage

- Debiasing should take care of leakage due to bias, also for large bias
- Debiasing data should not induce additional leakage: $I(S ; W) = I(S ; (W, D))$

4. Reusability

Classic code-offset construction is reusable (cf. Boyen, ACM-CCS-2004):

one enrollment leaks the same as many enrollments: $I(S ; W) = I(S_i ; (W_1, W_2, \dots))$

It would be nice to keep this property: $I(S ; (W, D)) = I(S_i ; (W_1, D_1, W_2, D_2, \dots))$

Debiasing Variant 1: “Classic” Von Neumann

Response X : 1 0 0 0 1 0 0 1 0 0 0 0 1 1 0 1 0 0
 von Neumann extraction: ≠ = ≠ = = = ≠ =
 Debaised Response Y : 1 1 0 0
 Debiasing Data D : 1 0 1 1 0 0 0 1 0

Consider consecutive pairs:

- Discard (0, 0) and (1, 1)
- Retain first bit of (0, 1) and (1, 0)
- Discard/retain choice is stored in debiasing data

1. Reliability: Bit error rate is hardly affected

Main advantage of Von Neumann-like methods!

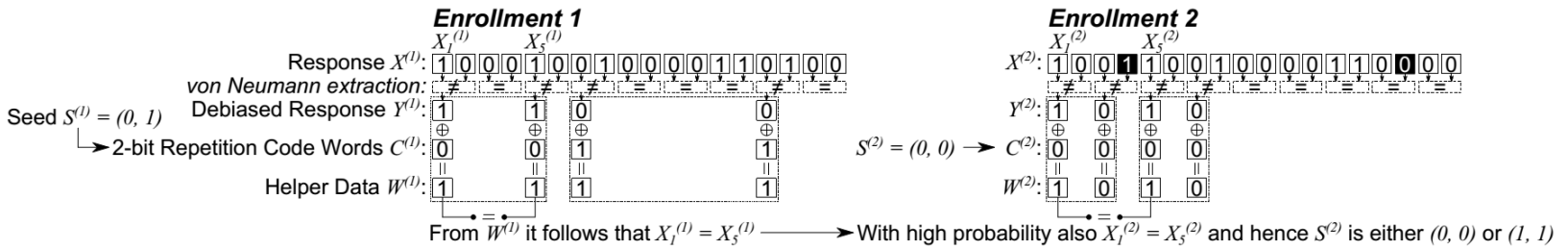
2. Efficiency: debiasing overhead factor > 4

Function of bias and reliability, e.g.: bias = 30% and $|Y| = 1000$ bits are needed with reliability $> 1 - 10^{-6}$, then $|X|$ needs to be $\geq 5334 \rightarrow$ overhead factor 5.3

3. Leakage: $I(S ; (W, D)) = 0$

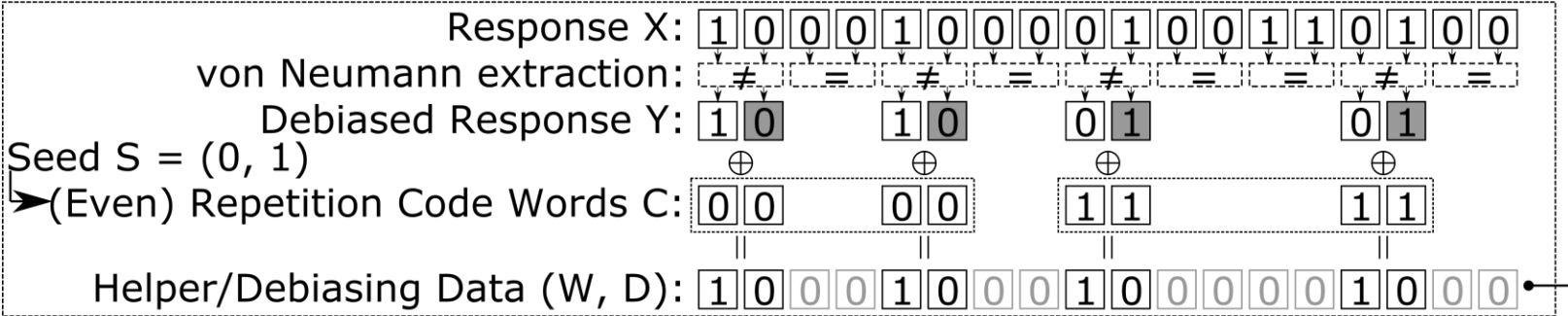
No more leakage, regardless of level of bias! (proof in full version)

4. Reusability: Not reusable! Due to stochastic nature caused by bit errors

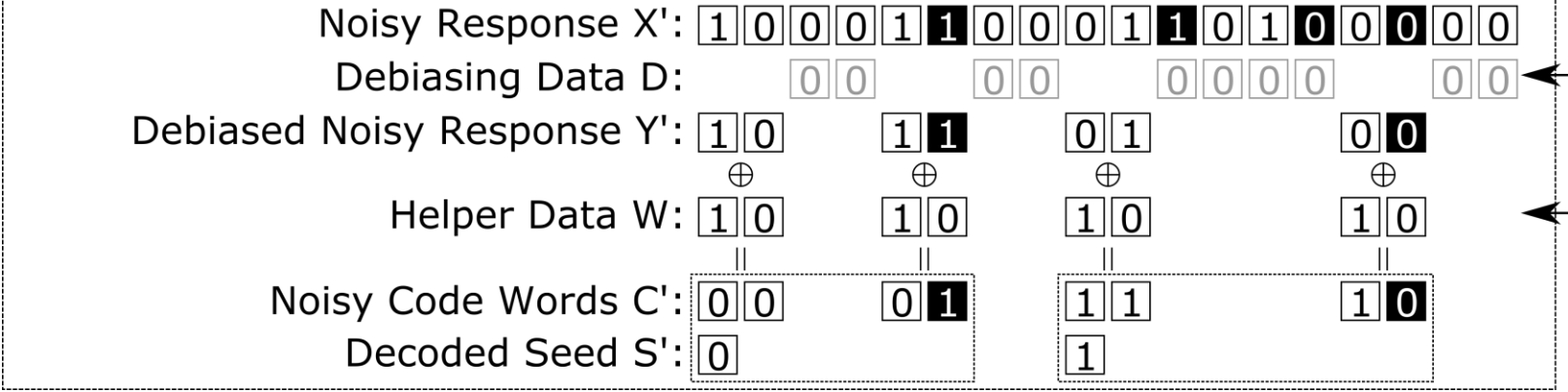


Debiasing Variant 2: Pair-Output Von Neumann

Enrollment



Reconstruction



- Same as classic V.N., but :
 - Retain full pairs instead of only first bit
 - Inner code is even-length repetition code



Debiasing Variant 2: Pair-Output Von Neumann

1. **Reliability:** Hardly affected (same as classic V.N.)
2. **Efficiency:** Improvement w.r.t classic V.N. with factor ~ 2 : debiasing overhead factor > 2

Function of bias and reliability, e.g.: bias = 30% and $|Y| = 1000$ bits are needed with reliability $> 1 - 10^{-6}$, then $|X|$ needs to be $\geq 2794 \rightarrow$ overhead factor 2.8

3. **Leakage:** $I(S ; (W, D)) = 0$

No leakage! Regardless of level of bias! (proof in full version)

Surprising given that Y has bit dependencies...

Trick: Entropy loss due to bit dependencies coincides exactly with entropy loss of repetition code \rightarrow no additional loss!

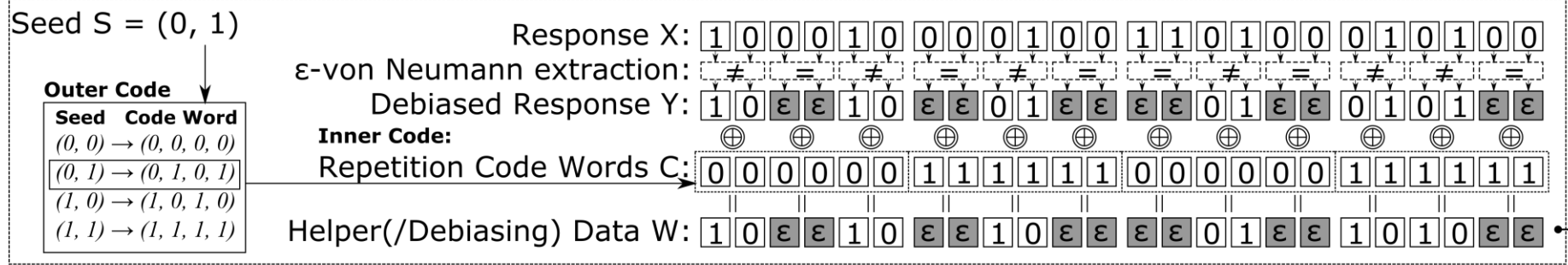
4. **Reusability:** Not reusable! (same as classic V.N.)

Variant 2+: *Multi-pass Tuple-Output Von Neumann*

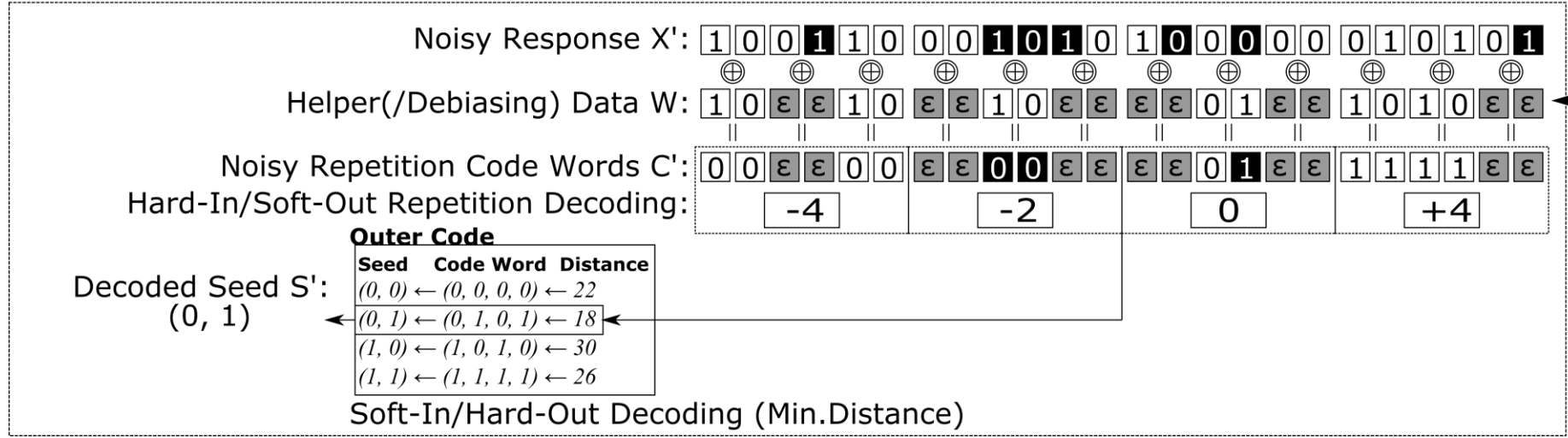
- Reconsider discarded bits in a new pass, now considering quadruplets...
- Same properties, but further improved efficiency: overhead factor 1.5

Debiasing Variant 3: Erasure Von Neumann

Enrollment



Reconstruction



- Same as pair-output V.N., but *erase* pairs i.s.o. discarding
 - Requires errors-and-erasures decoding at reconstruction



Debiasing Variant 3: Erasure Von Neumann

1. **Reliability:** Affected by introduction of erasures!

Better code needed

2. **Efficiency:** No bits are discarded, but code rate is affected to deal with additional erasures

Reliability and efficiency need to be considered together...

3. **Leakage:** $I(S ; (W, D)) = I(S ; W) = 0$

No leakage! Regardless of level of bias! (proof in full version)

4. **Reusability:** Reusable! (proof in full version)

Debiasing is no longer stochastic (not affected by eventual bit errors)

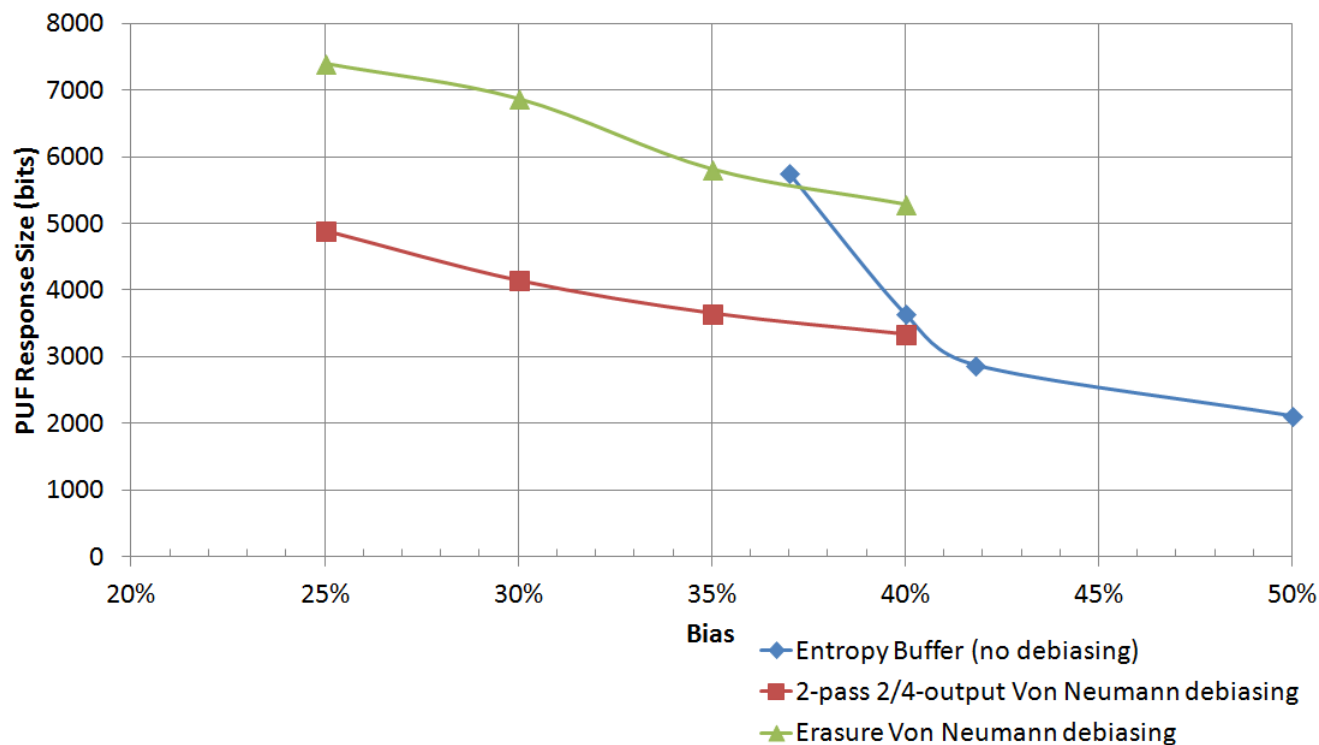
Variant 3+? No!

- As this will compromise reusability again



Comparison of Solutions

- Fair comparison:
 - Channel model: 0-bits and 1-bits have a different error rate
 - Error-rate and bias are related: e.g. 100% biased PUF must have error rate 0%
- Comparison based on repetition-Golay key generator:
(128-bit key, 15% noise, $1-10^{-6}$ reliability)



Concluding Remarks

- PUF error rate and bias (unpredictability) are equally important and closely related metrics
- PUF bias might cause entropy leakage and affect security of key generator:
 - Earlier constructions are not always secure for biased PUFs
 - Entropy buffer solution works for small bias (close to 50%), but does not scale
- We proposed debiasing solutions based on Von Neumann:
 - No more entropy leakage, regardless of bias level!
 - Overhead cost can be reduced by clever optimizations (pair output, multi-pass)
 - Bias outside [40%-60%]: debiasing is better than entropy buffer
 - Maintaining reusability comes at a cost
- Future work:
 - Improve efficiency, in particular combined with reusability
 - Other leakage models (bit correlations, ...)





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Full version of the paper: <https://eprint.iacr.org/2015/583.pdf>